

M.I. Maximum Revenue

Do Now:

Given the system of 2 equations, use algebra to create one equation in standard form.

$$3x^2 + 2y^2 - 54y - 143 = 0$$

$$x = 3y + 3$$

$$(3y+3)(3y+3)$$

$$9y^2 + 9y + 9y + 9$$

FoIL $3(3y+3)^2 + 2y^2 - 54y - 143 = 0$

$$3(9y^2 + 18y + 9) + 2y^2 - 54y - 143 = 0$$

$$\rightarrow 27y^2 + 54y + 27 + 2y^2 - 54y - 143 = 0$$

$$\frac{29y^2}{29} - \frac{116}{29} = \frac{0}{29} \quad \leftarrow$$

$$y^2 - 4 = 0$$

$$(y+2)(y-2) = 0$$

$$y = -2$$

$$y = 2$$

Find x

Find x

- What is **revenue**?

Revenue is the amount of \$ a company brings in.

The revenue of a product or service can depend on its price in two ways.

1. An increase in price means that more revenue per unit is earned but less units are sold.
2. A decrease in price means that less revenue is earned per unit but more units are sold.

In the next problems, a current price and sales amount will be given and how a price increase or decrease will affect the sales level.

A cinema multiplex averages 2000 tickets sold on a Saturday when ticket prices are \$8. A research firm has determined that for each \$0.25 increase in the ticket price, 50 fewer tickets will be sold.

What is the maximum revenue and what ticket price maximizes the revenue?

$$\begin{aligned}
 x=1 \text{ increase} &= \frac{\$ 8.25}{}, \frac{1950 \text{ tickets}}{} \\
 x=2 \text{ increases} &= \frac{\$ 8.50}{}, \frac{1900 \text{ tickets}}{} \\
 &\dots
 \end{aligned}$$

Let x = # of \$0.25 ticket increases

$$\rightarrow \frac{8 + .25x}{}$$
 = Ticket price (linear)

$$\rightarrow \frac{2000 - 50x}{}$$
 = Avg # of Tickets sold

To Get Revenue:

- Ticket Revenue: multiply $\frac{\# \text{ tickets sold}}{}$ \times $\frac{\text{cost per ticket}}{}$

$$\underline{R(x) = -12.5x^2 + 100x + 16,000}$$